# H<sup>3</sup>DP: Triply-Hierarchical Diffusion Policy for Visuomotor Learning

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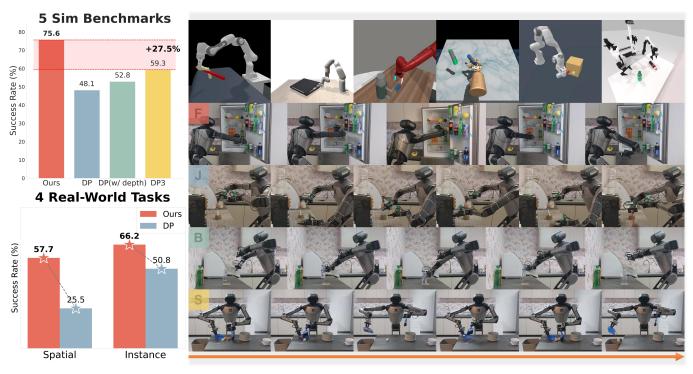


Fig. 1: **H**<sup>3</sup>**DP** can not only achieve superior performance across 44 tasks on 5 simulation benchmarks, but also handle long-horizon challenging manipulation tasks in cluttered real-world scenarios.

Abstract—Visuomotor policy learning has witnessed substantial progress in robotic manipulation, with recent approaches predominantly relying on generative models to model the action distribution. However, these methods often overlook the critical coupling between visual perception and action prediction. In this work, we introduce Triply-Hierarchical Diffusion Policy (H<sup>3</sup>DP), a novel visuomotor learning framework that explicitly incorporates hierarchical structures to strengthen the integration between visual features and action generation. H<sup>3</sup>DP contains 3 levels of hierarchy: (1) depth-aware input layering that organizes RGB-D observations based on depth information; (2) multi-scale visual representations that encode semantic features at varying levels of granularity; and (3) a hierarchically conditioned diffusion process that aligns the generation of coarse-to-fine actions with corresponding visual features. Extensive experiments demonstrate that  $H^3DP$  yields a +27.5% average relative improvement over baselines across 44 simulation tasks and achieves superior performance in 4 challenging bimanual real-world manipulation tasks. Project Page: https://lyy-iiis.github.io/h3dp/.

# I. INTRODUCTION

Visuomotor policy learning has emerged as a prevailing paradigm in robotic manipulation [6, 65, 5, 62, 60]. Existing approaches have increasingly adopted powerful generative methods, such as diffusion and auto-regressive models, to model the action generation process [34, 57, 11, 45, 22]. However, these predominant methods have focused primarily on separately refining either the representation of perception or actions, often overlooking establishing a tight correspondence between perception and action. In contrast, human decisionmaking inherently involves hierarchical processing of information from perception to action [18, 3]. The visual cortex extracts features in a layered fashion and performs hierarchical inference based on visual motion perception, ultimately resulting in the generation of structured motor behaviors [23, 4]. Inspired by this, we argue that enabling learned visuomotor agents to emulate such hierarchical behavior patterns is also critical for

enhancing their decision-making capabilities.

Prior works have primarily focused on hierarchically modeling the action generation process alone [50, 13], without explicitly incorporating hierarchical structure throughout the whole visuomotor policy pipeline. In this paper, we present  $\mathbf{H}^{3}\mathbf{DP}$ , a novel visuomotor policy learning framework grounded in three levels of hierarchy: input, representation, and action generation. This design reflects the hierarchical processing mechanisms that humans use the visual cortex to perceive environmental stimuli to guide motor behavior.

At the input level, to better leverage the depth information in modern robotic benchmarks and datasets [19, 27, 44, 12], H<sup>3</sup>DP moves beyond prior 2D approaches that primarily rely on RGB or simple RGB-D concatenation, which has shown limited effectiveness in prior work [62, 67]. We introduce **depth-aware layering** strategy that partitions the RGB-D input into distinct layers based on depth cues. This approach not only enables the policy to explicitly distinguish between foreground and background, but also suppresses distractors and occlusions [37, 1], thereby enhancing the understanding and reasoning of spatial structure in the cluttered visual scenarios.

For visual representation, to address the limitations of flattening image features into a single vector, which can discard some spatial structures and semantic information [15, 41, 25], H<sup>3</sup>DP employs **multi-scale visual representation**, where different scales capture features at varying granularity levels, ranging from global context to fine visual details.

In the action generation stage, H<sup>3</sup>DP incorporates a key inductive bias inherent to the diffusion process: the tendency to progressively reconstruct features from low-frequency to high-frequency components [40, 8, 55], by **hierarchical action generation**. Specifically, coarse visual features guide initial denoising steps to shape the global structure (low-frequency components) of action, while fine-grained visual features inform the later steps to refine precise details (high-frequency components). This establishes a tighter coupling between action generation and visual encoding, enabling the policy to generate actions that are semantically grounded in multi-scale perceptual features.

We validate  $\mathrm{H}^3\mathrm{DP}$  through extensive experiments on 44 simulation tasks across 5 diverse benchmarks, where it surpasses state-of-the-art methods by a relative average margin of +27.5%. Furthermore, in real-world evaluations, we deploy bimanual robotic systems to tackle four challenging tasks situated in cluttered environments, involving high disturbances and long-horizon objectives.  $\mathrm{H}^3\mathrm{DP}$  achieves a +32.3% performance improvement over Diffusion Policy in these real-world scenarios.

# II. RELATED WORK

Visual imitation learning. Numerous studies have proposed efficient policy learning algorithms from different aspects [6, 65, 58]. As a representative approach, to endow the learned policy multi-modality ability, Diffusion Policy [6] incorporates the diffusion process to better represent the action distribution. Based on DP, methods like DP3 [62, 61] and 3D-Actor [20],

designed for point cloud inputs, enhance the policy's scene understanding by refining the visual representation. Consistency Policy [34] and ManiCM [30] modify the inference process to achieve the inference acceleration. However, these approaches focus solely on enhancing either the action generation or the visual feature extraction, without explicitly modeling the relationship between them. To address this issue, we propose a hierarchical framework that couples multi-scale visual representations with the diffusion process, enabling a more structured integration between visual features and action generation.

Leveraging hierarchical information for policy learning. In the computer vision community, numerous studies have leveraged hierarchical information to address a variety of downstream tasks [53, 56, 24, 38, 29, 42]. For example, standard diffusion models [48, 17, 47, 49] and flow matching [26, 28, 10] adopt the U-Net framework [41, 66], which exploits multi-scale feature representations to retain rich contextual information throughout the denoising process. VAR [52] innovatively employs multi-scale visual representations with quantization to perform image generation in an auto-regressive manner. In robot learning, recent works [13, 33, 64] have also begun to adopt hierarchical paradigms for policy learning. Dense Policy [50] leverages a bidirectional extension strategy to enable hierarchical action prediction. ARP [64] predicts a sequence of actions at different levels of abstraction in a hierarchical way. CARP [13] draws inspiration from VAR by employing a multi-scale VQ-VAE [53, 38] to construct action sequences and subsequently generating residual actions autoregressively using a GPT-style architecture [35]. However, these algorithms model only the hierarchical structure of the action generation process, without explicitly addressing the crucial linkage between visual representation and action in visuomotor policy learning. In contrast, H<sup>3</sup>DP not only incorporates multi-scale visual representations but also leverages the inherent strengths of diffusion models to seamlessly integrate coarse-to-fine action generation into the diffusion process itself. Furthermore, by adopting a depth-aware layering strategy, H<sup>3</sup>DP maximizes the utilization of hierarchical feature information across the input, latent, and output stages, thereby enriching the policy learning pipeline in a structured and semantically aligned manner.

#### III. METHOD

We employ three hierarchical structures to enhance the policy's understanding of visual input and predict more accurate action distributions. At the input level, the RGB-D image is discretized into multiple layers to improve the policy's ability to distinguish and interpret foreground-background variations. Upon this, we adopt a multi-scale visual representation, wherein coarse-grained features capture global contextual information, while fine-grained features encode detailed scene attributes. On the action side, correspondingly, the representations at different scales are utilized to generate actions in a coarse-to-fine manner, thus strengthening the correlation between action and visual representations. A detailed discussion of each part will be provided in the following sections.

# A. Depth-aware Layering

Effective robotic manipulation hinges on robust spatial understanding. While RGB data provides rich texture and color information, depth supplies the critical geometric context, including the relative spatial arrangement of objects and their distances. Combining these modalities offers a powerful foundation for scene comprehension. However, simply concatenating RGB images with depth maps does not lead to performance improvements [62, 67]. Hence, to fully exploit the geometric structure inherent in depth maps, we introduce a depth-aware layering mechanism inspired by Zhang et al. [63]. Pixels with depth d are assigned to layer m using linear-increasing discretization:

$$m = \left[ -0.5 + 0.5\sqrt{1 + 4(N+1)(N+2)\frac{d - d_{\min}}{d_{\max} - d_{\min} + \epsilon}} \right],$$

which promotes the robot to focus more on its workspace. By explicitly encoding objects distributed across different depth planes, this structured representation retains all visual detail while strategically utilizing depth to impose a meaningful foreground-background separation, thereby enabling the policy to selectively attend to different regions of the image. This design can effectively boost the agent's capacity for spatial perception and interaction planning. Furthermore, we also conduct comparisons against other discretization algorithms and perform additional experiments to substantiate the effectiveness of our proposed depth-aware layering method. The corresponding results are provided in Appendix E3 and Appendix E7.

# B. Multi-Scale Visual Representation

In visuomotor policy learning, visual representation plays a crucial role in embedding input images and mapping them to actions. An effective visual encoder should capture various granularity features of the visual scenarios and guide the policy to predict the action distribution. However, existing methods typically extract features at a single spatial scale or compress them into a fixed-resolution representation, limiting the expressiveness of learned features [15, 41, 25]. To address this problem, we hierarchically partition the feature map into multiple scales, enabling the capture of both coarse structural information and detailed local cues.

**Interpolation and Quantization.** After applying depth-aware layering to the input image I, each layer  $I_m$  is independently encoded into multi-scale feature maps  $\{f_{m,k}|f_{m,k}\in\mathbb{R}^{h_k\times w_k\times C}\}_{k=1}^K$ , where  $\{(h_k,w_k)\}_{k=1}^K$  denotes the spatial resolutions across scales. Adopting the quantization design in VQ-VAE [53, 38], these feature maps  $\{f_{m,k}\}_{k=1}^K$  are quantized into discrete vectors drawn from a learnable codebook  $\mathcal{Z}_m\in\mathbb{R}^{V\times C}$ . Specifically, each feature vector  $f_{m,k}^{(i,j)}$  is mapped to its nearest neighbor in Euclidean distance:

$$f_{m,k}^{(i,j)} \leftarrow \underset{z \in \mathcal{Z}_m}{\arg \min} \|z - f_{m,k}^{(i,j)}\|_2.$$
 (2)

By applying differentiable interpolation and lightweight convolution to the quantized features  $f_{m,k}$ , we then obtain the

multi-scale visual representations  $\{\hat{f}_{m,k}\}_{k=1}^{K}$  for each layer  $I_m$ . The pseudocode of full encoding procedure is detailed in Algorithm 1, Appendix B.

**Training.** To ensure consistent representations across scales, we aim to minimize the consistency loss between the original feature  $f_m = \mathcal{E}_m(I_m)$  and the representation  $\hat{f}_{m,k}$  at different scales:

$$\mathcal{L}_{\text{consistency}} = \sum_{m=0}^{N-1} \sum_{k=1}^{K} \left( \left\| \hat{f}_{m,k} - \text{sg}(f_m) \right\|_{2}^{2} + \beta \left\| f_m - \text{sg}(\hat{f}_{m,k}) \right\|_{2}^{2} \right),$$
(3)

where  $\operatorname{sg}(\cdot)$  is the stop gradient operator and  $\beta$  balances the gradient flow between two terms. The visual encoder  $\{\mathcal{E}_m\}_{m=0}^{N-1}$  and codebook  $\{\mathcal{Z}_m\}_{m=0}^{N-1}$  are trained end-to-end, as described in detail in Appendix B.

# C. Hierarchical Action Generation

To match the inherent inductive biases of denoising process [40, 8, 55], we leverage multi-scale visual representations to model action generation in a coarse-to-fine manner. The early stage actions are derived from representations that capture global scene information, while fine-grained representations are responsible for generating detailed action components. This approach couples the visual representation and the action generation process via reinforcing their correspondence at the same hierarchical levels.

**Inference.** Our action generation module is a denoising diffusion model conditioned on multi-scale features  $F = \{\hat{f}_k = \{\hat{f}_{m,k}\}_{m=0}^{N-1}\}_{k=1}^K$  and robot poses q. The denoising process unfolds over T steps partitioned into K stages  $\bigcup_{k=1}^K (\tau_{k-1}, \tau_k]$ . When  $t \in (\tau_{k-1}, \tau_k]$ , the denoising network  $\epsilon_{\theta}^{(t)}$  conditioning on the corresponding feature map  $\hat{f}_k$  and robot poses q, predicts the noise component

$$\epsilon^t = \epsilon_\theta^{(t)}(a^t | \hat{f}_k, q), \tag{4}$$

then generates  $a^{t-1}$  from  $a^t$  via:

$$a^{t-1} = \sqrt{\alpha_{t-1}} \left( \frac{a^t - \sqrt{1 - \alpha_t} \cdot \epsilon^t}{\sqrt{\alpha_t}} \right) + \sqrt{1 - \alpha_{t-1} - \sigma_t^2} \cdot \epsilon^t + \sigma_t \tilde{\epsilon}^t,$$
(5)

gradually transforming the Gaussian noise  $a^T$  into the noise-free action  $a^0$ , where  $\alpha_t$ ,  $\sigma_t$  are fixed parameters depending on the noise scheduler, and  $\tilde{\epsilon}^t \sim \mathcal{N}(0,\mathbf{I})$  is a Gaussian noise.

**Training.** To train the denoising network  $\epsilon_{\theta}^{(t)}$ , we randomly sample an observation-action pair  $((I,q),a^0)\in\mathcal{D}$  and noise  $\epsilon\sim\mathcal{N}(0,\mathbf{I})$ . The network is optimized to predict  $\epsilon$  given a noisy action conditioned on the final feature map  $\hat{f}_K$  and robot pose q, via the objective:

$$\mathcal{L}_{\text{diffusion}} = \mathbb{E}_{a^0, \epsilon, t} \left[ \gamma_t \| \epsilon_{\theta}^{(t)} (\sqrt{\alpha_t} a^0 + \sqrt{1 - \alpha_t} \epsilon | \hat{f}_K, q) - \epsilon \|^2 \right], \tag{6}$$

where  $\{\gamma_t\}$  are pre-defined coefficients. More implementation details can be found in Appendix A. By conditioning on the final feature  $\hat{f}_K$  during training, gradients from the loss propagate through the entire hierarchical encoder, implicitly optimizing all  $\{\hat{f}_k\}_{k=1}^K$ . This design promotes consistency

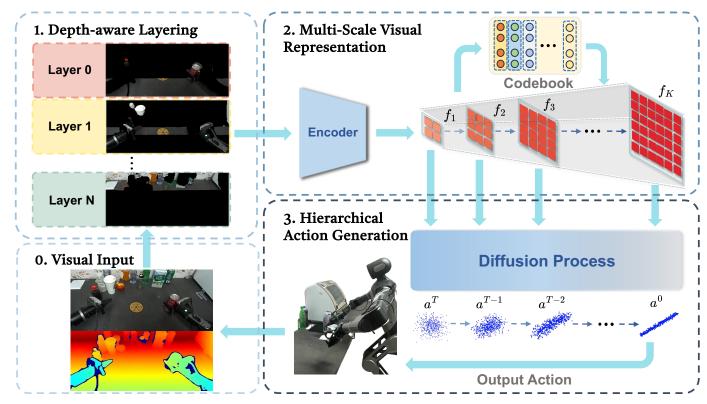


Fig. 2: **Overview of H³DP**. H³DP integrates three hierarchical design principles across the perception and action generation pipeline. At the input level, RGB-D images are decomposed into multiple layers based on their depth values. Then, we employ multi-scale visual representations to capture features at varying levels of granularity. During the action generation, denoising process is divided into several stages guided by multi-scale visual representations.

of representations at each scale for action generation while enhancing training efficiency.

**Discussions.** Diffusion models inherently aim to predict the posterior average of the target distribution conditioned on the provided features [7, 51], i.e., the optimal denoising network  $\epsilon_{\theta^*}^{(t)}$  follows  $\epsilon_{\theta^*}^{(t)}(a^t|f,q) = \mathbb{E}_{t,\epsilon,a^0,\sqrt{\alpha}_ta^0+\sqrt{1-\alpha}_t\epsilon=a^t}[\epsilon|a^t,f,q]$ . Features at varying resolutions retain information across distinct frequency domains. Consequently, they provide robust guidance for generating specific frequency components of the action during relevant stages of the denoising process. Related experiments are shown in Section IV-A3. By using lower-resolution features for earlier stages and gradually refining the predictions with higher-resolution features, the model benefits from both the stability of coarse representations and the precision of fine details.

#### IV. EXPERIMENTS

In this section, we present extensive experiments across simulated and real-world settings to demonstrate the efficacy of H<sup>3</sup>DP. In addition, we perform thorough ablation analyses to evaluate the contribution of each hierarchical design.

#### A. Simulation Experiments

1) Experiment setup: Simulation benchmarks and baselines: To sufficiently verify the effectiveness of H<sup>3</sup>DP, we evaluate H<sup>3</sup>DP on 5 simulation benchmarks, encompassing a total of 44 tasks. These tasks span a variety of manipulation

challenges, including articulated object manipulation [2, 36, 59], deformable object manipulation [14], bimanual manipulation [31], and dexterous manipulation [2, 36]. The details of the expert demonstrations can be found in Appendix C. To comprehensively assess the performance of H<sup>3</sup>DP, we compare it against three baselines: *Diffusion Policy* [6], one of the most widely used visuomotor policy learning algorithms; *Diffusion Policy (w/ depth)*, which extends Diffusion Policy to incorporate RGB-D input to bridge the information gap; and *DP3* [62], an enhanced version of Diffusion Policy that leverages an efficient encoder for point cloud input.

**Evaluation metric:** Each experiment is run with three different seeds to mitigate performance variance. For each seed, we evaluate 20 episodes every 200 training epoches. In simpler MetaWorld, Adroit and DexArt tasks, we compute the average of the highest five success rates as its success rate, while in other environments, only the hightest success rate is recorded.

2) Simulation performance: As shown in Table I, the simulation experiment results exhibit that H<sup>3</sup>DP outperforms or achieves comparable performance among the whole simulation benchmarks. Our method outperforms DP3 by a relative average margin of +27.5%. Notably, DP3 requires manual segmentation of the point cloud to remove background and task-irrelevant elements. This process introduces additional human effort and renders performance susceptible to segmentation quality. Relevant experimental results are provided in Appendix E6. In

TABLE I: Simulation task results. Across 5 simulation benchmarks with various difficult levels,  $H^3DP$  obtains +27.5% relative performance gains on average over 44 tasks.

Method \ Tasks	MetaWorld (Medium 11)	MetaWorld (Hard 5)	MetaWorld (Hard++ 5)	ManiSkill (Deformable 4)	ManiSkill (Rigid 4)	Adroit (3)	DexArt (4)	RoboTwin (8)	Average (44)
H <sup>3</sup> DP	98.3	87.8	95.8	59.3	65.3	87.3	53.3	57.4	$75.6{\pm}18.6$
DP	78.2	52.6	58.0	22.3	27.5	79.0	44.3	22.8	$48.1 \pm 23.1$
DP (w/ depth)	77.7	57.2	71.2	44.5	40.8	76.0	42.0	12.6	$52.8 \pm 22.2$
DP3	89.1	52.6	88.4	26.5	33.5	84.0	54.8	45.9	$59.3 \pm 24.9$

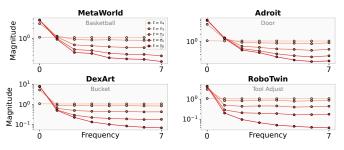


Fig. 3: Action DFT results. As the denoising process progresses, the Gaussian noise  $(t=\tau_4)$  is gradually transformed into the predicted action  $(t=\tau_0)$ . Timesteps  $\tau_i$  is arranged in descending order of noise levels. The results reveal a consistent frequency evolution pattern: low-frequency components predominantly emerge during the early stages of denoising, whereas high-frequency features are progressively introduced in the latter phases of the process.

contrast, benefiting from our design, H<sup>3</sup>DP obtains superior performance using only raw RGB-D input, without the need for segmentation and human effort. Furthermore, on the Adroit and DexArt benchmark, while DP3 leverages multi-view cameras to restore the complete point clouds, H<sup>3</sup>DP attains comparable performance using only one single-camera RGB-D image. The whole simulation results in each task can be found in Appendix E1.

3) Spectral analysis of actions: To gain a more comprehensive understanding of the action generation, we apply Discrete Fourier Transform (DFT) to examine how the frequency composition of actions evolves throughout the denoising process. Specifically, we conduct the analysis across 4 benchmarks and visualize the spectral characteristics of action chunks during generation. As shown in Figure 3, the results consistently indicate that the denoising process begins with the synthesis of low-frequency features, which are incrementally complemented by higher-frequency features in later stages. This observation not only shows that action, akin to image, exhibits an intrinsic inductive bias in the diffusion process, but also elucidates the action generation mechanism of H<sup>3</sup>DP, wherein actions are hierarchically composed to captured features across varying levels of granularity.

# B. Real-world Experiments

In terms of real-world experiments, we choose Galaxea R1 robot as our platform. We design four diverse challenging real-world tasks to evaluate the effectiveness of our method:

Clean Fridge (CF): In a cluttered refrigerator environment,

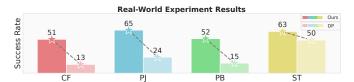


Fig. 4: **Success rate in real-world.** Dark-colored bars correspond to H<sup>3</sup>DP, whereas the light-colored bars correspond to DP. H<sup>3</sup>DP outperforms DP in all 4 challenging real-world tasks.

the robot is required to relocate a transparent bottle from the upper compartment to the lower one. The bottle is randomized within a  $30~\text{cm} \times 5~\text{cm}$  region on both the upper and lower shelves of the refrigerator.

**Pour Juice (PJ):** This is a long-horizon task. The robot is required to place a cup in front of a water dispenser, scoop a spoonful of juice powder, then fill the cup with water, and finally put a straw in the cup. The cup is placed within a 7 cm  $\times$  7 cm area, and both the color of the juice powder and the position of the water dispenser are subject to variation across trials.

**Place Bottle (PB):** The robot must place a bottle, initially located at a random position, onto a designated coaster. The bottle is placed within a 15 cm  $\times$  15 cm region, while the coaster is positioned within an around 25 cm  $\times$  25 cm area. **Sweep Trash (ST):** This long-horizon task entails picking up a broom, sweeping scattered debris on a table into a dustpan, and subsequently emptying the contents into a trash bin. The trash is randomly distributed across the entire table surface, approximately within a 40 cm  $\times$  40 cm area.

1) Experiment Setup: We use the ZED camera to acquire the depth 60Hz image with running frequency. demonstrations are collected by Meta

Regarding

Quest3.



Fig. 5: Experiment Setup.

the two long-horizon tasks, both the baseline and our method incorporate the pre-trained ResNet18 [16] encoders for RGB modality to enhance the policy's perceptual capabilities in real-world environments. Each task is evaluated at 20 randomly sampled positions within the defined randomization range for each method. We record the success trials and calculate the corresponding success rate. In addition, during

policy deployment, we adopt an *asynchronous* design to obtain an approximately 15Hz inference speed. We also introduce *temporal ensembling* and *p-masking* to improve temporal consistency and alleviate overfitting to the proprioception state. More setup details can be found in Appendix D.

2) Experiment Results: Spatial generalization: As shown in Figure 4, H<sup>3</sup>DP significantly outperforms the baseline across all four real-world tasks, achieving an average improvement of +32.3%. It should be noted that in CF and PJ tasks, the policy is required to not only identify target objects in cluttered visual environments but also perform long-horizon reasoning to accomplish the tasks. While DP struggles to complete either task, H<sup>3</sup>DP achieves substantial improvements, outperforming DP by +38% and +41% respectively. Therefore, H<sup>3</sup>DP demonstrates superior perceptual and decision-making capabilities compared to alternative algorithms. Meanwhile, it should be noted that in terms of the point cloud based method DP3, it requires precise segmentation and high-fidelity depth sensing, resulting in it being less effective in handling our four cluttered real-world scenes that we designed. Comparative experimental results for DP3 are presented in Appendix E8.

**Instance generalization:** Regarding instance generalization, we evaluate the model on two real-world tasks by varying the size and shape of bottles or trash items. As shown in Table II, after replacing the objects with variants of differing sizes and shapes, H<sup>3</sup>DP maintains strong generalization capabilities attributable to its ability to hierarchically model features at multiple levels of granularity, and consistently outperforms baseline approaches across all settings.

TABLE II: Instance generalization results.  $\mathrm{H}^3\mathrm{DP}$  achieves +15.4% performance gain.

Method \ Tasks	Place Bottle coke bottle sprite can			8 cm <sup>3</sup>	Average		
H <sup>3</sup> DP	67	49	53	75	86	67	66.2
Diffusion Policy	45	36	40	52	72	60	50.8

# C. Ablation Study

In this section, we ablate each key component of our framework and conduct experiments on three benchmarks to further exhibit the effectiveness of H<sup>3</sup>DP. The entire results in each benchmark can be found in Appendix E2.

Each hierarchical design. We ablate the three hierarchical components introduced in our framework and compare them against the baseline Diffusion Policy with RGB-D input. As shown in Table III, each hierarchical component independently contributes to performance improvement, consistently outperforming the DP (w/ depth). Furthermore, Table III also demonstrates that the integration of all three hierarchical designs leads to a substantial enhancement in overall performance.

The choice of N in depth-aware layering. For the depth-aware layering component, we investigate whether the policy's performance is sensitive to the choice of the number of layers N. As presented in Table IV, the trained policy achieves optimal and comparable performance when N is set to 3 or 4, a trend consistently observed across all evaluated benchmarks. When N

TABLE III: Ablation on hierarchical features.

Methods \ Benchmarks	MW	MS	RT	Average
H <sup>3</sup> DP	65.7	68.0	45.0	59.6
w/o depth layering	55.0	52.5	32.0	46.5
w/o hierarchical action	57.0	50.0	40.0	49.0
w/o multi-scale representation	53.7	52.5	40.0	48.7
DP (w/ depth)	46.7	47.5	32.0	42.1

becomes excessively large, the image is over-partitioned, thus reducing the representation capacity of the policy. Nevertheless, even in such cases, the performance remains slightly better than the non-layered baseline. These findings highlight the critical role of depth-aware layering in enhancing policy effectiveness.

TABLE IV: Ablation on number of layers N.

Methods \ Benchmarks	MW	MS	RT	Average
$H^3DP (N=1)$	55.0	52.5	32.0	46.5
$H^3DP (N=2)$	55.7	60.0	35.0	50.2
$H^3DP (N=3)$	65.7	68.0	45.0	59.6
$H^3DP (N=4)$	67.0	61.5	50.0	59.5
$H^3DP (N=5)$	58.7	55.0	50.0	54.6
$H^3DP (N=6)$	56.0	51.0	40.0	49.0

#### V. CONCLUSION

In this paper, we introduce H³DP, an efficient generalizable visuomotor policy learning framework that can obtain superior performance in a wide range of simulations and challenging real-world tasks. Extensive empirical evidence suggests that establishing a more cohesive integration between visual feature representations and the action generation process can enhance the generalization capacity and learning efficiency of our learned policies. The proposed three hierarchical designs not only facilitate the effective fusion of RGB and depth modalities, but also strengthen the correspondence between visual features and the generated actions at different granularity levels. In the future, we expect to extend the applicability of H³DP to more intricate and fine-grained dexterous real-world tasks.

#### VI. LIMITATIONS

Although H³DP has demonstrated effectiveness in a variety of tasks, there exist several limitations. First, despite our use of asynchronous execution to improve inference speed in real-world settings, the overall inference time of diffusion-based models remains relatively slow. We could explore distilling the policy into a consistency model, to enhance real-time performance. Second, the limited depth quality of the ZED camera may hinder the policy's full potential in real-world deployment; employing higher-fidelity depth sensors could further boost the effectiveness of H³DP in practical scenarios.

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#### **APPENDIX**

# A. Hyperparameters

To effectively address the varying levels of difficulty and distinct properties inherent to different benchmarks, we adapt our hyperparameter settings for each specific dataset. The chosen configurations, detailed in Table V, VI, VII, VIII, are selected based on previous works [6, 62, 67, 31].

TABLE V: Hyperparameters used for MetaWorld, DexArt.

Hyperparameter	Value
Observation Horizon $(T_o)$	2
Action Horizon $(T_a)$	2
Prediction Action Horizon $(T_p)$	4
Optimizer	AdamW [21]
Betas $(\beta_1, \beta_2)$	[0.95, 0.999]
Learning Rate	1.0e-4
Weight Decay	1.0e-6
Learning Rate Scheduler	Cosine
Training Timesteps $(T)$	50
Inference Timesteps	20
Prediction Type	$\epsilon$ -prediction
Image Resolution	$128 \times 128$
Scale Number (K)	4
Multi-Scale Representation Resolutions $(\{(h_k, w_k)\}_{k=1}^K)$	{(1,1),(3,3),(5,5),(7,7)}
Stage Boundiaries $(\{\tau_k/T\}_{k=0}^K)$	{0,0.4,0.6,0.8,1.0}

TABLE VI: Hyperparameters used for Adroit.

Hyperparameter	Value
Observation Horizon $(T_o)$	2
Action Horizon $(T_a)$	2
Prediction Action Horizon $(T_p)$	4
Optimizer	AdamW
Betas $(\beta_1, \beta_2)$	[0.95, 0.999]
Learning Rate	1.0e-4
Weight Decay	1.0e-6
Learning Rate Scheduler	Cosine
Training Timesteps $(T)$	50
Inference Timesteps	20
Prediction Type	$\epsilon$ -prediction
Image Resolution	84 × 84
Scale Number $(K)$	4
Multi-Scale Representation Resolutions ( $\{(h_k, w_k)\}_{k=1}^K$ )	{(1,1),(3,3),(5,5),(6,6)}
Stage Boundiaries $(\{\tau_k/T\}_{k=0}^K)$	{0,0.4,0.6,0.8,1.0}

 $TABLE\ VII:\ \textbf{Hyperparameters}\ \textbf{used}\ \textbf{for}\ \textbf{ManiSkill.}$ 

Hyperparameter	Value
Observation Horizon $(T_o)$	2
Action Horizon $(T_a)$	8
Prediction Action Horizon $(T_p)$	16
Optimizer	AdamW
Betas $(\beta_1, \beta_2)$	[0.9, 0.95]
Learning Rate	1.0e-4
Weight Decay	1.0e-4
Learning Rate Scheduler	One Cycle LR [46]
Training Timesteps $(T)$	100
Inference Timesteps	100
Prediction Type	$\epsilon$ -prediction
Image Resolution	$128 \times 128$
Scale Number $(K)$	4
Multi-Scale Representation Resolutions $(\{(h_k, w_k)\}_{k=1}^K)$	{(1,1),(3,3),(5,5),(7,7)}
Stage Boundaries $(\{\tau_k\}_{k=0}^K/T)$	{0,0.4,0.6,0.8,1.0}

TABLE VIII: Hyperparameters used for RoboTwin.

Hyperparameter	Value
Observation Horizon $(T_o)$	3
Action Horizon $(T_a)$	2
Prediction Action Horizon $(T_p)$	8
Optimizer	AdamW
Betas $(\beta_1, \beta_2)$	[0.95, 0.999]
Learning Rate	1.0e-4
Weight Decay	1.0e-6
Learning Rate Scheduler	Cosine
Training Timesteps $(T)$	100
Inference Timesteps	100
Prediction Type	$\epsilon$ -prediction
Image Resolution	$180 \times 320$
Scale Number $(K)$	4
Multi-Scale Representation Resolutions $(\{(h_k, w_k)\}_{k=1}^K)$	{(1,3),(3,5),(5,7),(5,9)}
Stage Boundaries $(\{\tau_k\}_{k=0}^K/T)$	{0,0.4,0.6,0.8,1.0}

In addition to the hyperparameters reported in the table, the choice of the number of layers N demonstrates great importance, as shown in Table IV. Empirically, we choose N=4 in Adroit, MetaWorld Hard and Hard++, and N=3 in other benchmarks. The noise scheduler for diffusion process is determined by  $\alpha_t$ , defined using function f(t)

$$\alpha_t = \frac{f(t)}{f(0)}, \quad \text{where} \quad f(t) = \cos^2\left(\frac{\pi}{2}\frac{t/T+s}{1+s}\right).$$
 (7)

Here, T is the total number of diffusion timesteps and s is an offset parameter.

For the reverse process, we employ different formulations depending on the environment. In MetaWorld, Adroit and DexArt, we follow the DDIM [47] approach, formulating the reverse process as an ODE, which corresponds to setting

$$\sigma_t = 0 \tag{8}$$

for all t. In ManiSkill and RoboTwin, we follow the design of DDPM [17] and formulate the reverse process as a Variance Preserving (VP) SDE [49]. In this case, for all t,

$$\sigma_t = \sqrt{\frac{1 - \alpha_{t-1}}{1 - \alpha_t}} \sqrt{1 - \frac{\alpha_t}{\alpha_{t-1}}}.$$
(9)

Furthermore, consider the weighting term  $\gamma_t$  in Equation 6. Since the choice of  $\gamma_t$  does not affect the optimal denoising network  $\epsilon_{\theta^*}$ , we set

$$\gamma_t = 1 \tag{10}$$

for all t.

# B. Method Details

This section outlines the implementation details of our multi-scale encoding. The encoder  $\mathcal{E}_m$  for each depth layer m adopts the architecture from VQGAN [9], ensuring strong representational capacity while preserving spatial information. We use interpolate to denote a differentiable resizing operation (e.g. bilinear or nearest-neighbor interpolation), which is crucial for enabling gradient flow during training. The function  $\mathcal Q$  represents the quantization process detailed in Equation 2. Finally, after interpolating a feature map  $f_{m,k}$  to the highest resolution, we apply a lightweight convolutional network  $\phi_{m,k}$  designed to help restore fine details from the potentially lower-resolution source features.

The pseudocode for this process is outlined in Algorithm 1.

# **Algorithm 1:** Multi-scale Encoding

```
1 Inputs: raw image I
 2 Hyperparameters: depth layer number N, scale number K, resolutions \{(h_k, w_k)\}_{k=1}^K
3 Partition image I into N+1 images \{I_m\}_{m=0}^N according to Equation 1
4 for m = 0, ..., N-1 do
          f_m \leftarrow \mathcal{E}_m(I_m) \in \mathbb{R}^{h_K \times w_K \times C}
 5
          for k = 1, \dots, K do
 6
               f_{m,k} \leftarrow \text{interpolate}(f_m, h_k, w_k) \in \mathbb{R}^{h_k \times w_k \times C}
 7
               f_{m,k} \leftarrow \mathcal{Q}(f_{m,k})
 8
               f_{m,k} \leftarrow \phi_{m,k}(\text{interpolate}(f_{m,k}, h_K, w_K)) \in \mathbb{R}^{h_K \times w_K \times C}

\hat{f}_{m,k} \leftarrow \sum_{k' \leq k} f_{m,k'} 

f_m \leftarrow f_m - \overline{f}_{m,k}

10
11
12 Return: multi-scale features F = \{\hat{f}_k = \{\hat{f}_{m,k}\}_{m=0}^{N-1}\}_{k=1}^K
```

All trainable parameters, including the visual encoders  $\{\mathcal{E}_m\}_{m=0}^{N-1}$ , the codebooks  $\{\mathcal{Z}_m\}_{m=0}^{N-1}$ , the CNN parameters  $\{\{\phi_{m,k}\}_{m=0}^{N-1}\}_{k=1}^{K}$ , and the denoising network  $\epsilon_{\theta}$ , are trained jointly in an end-to-end manner. The optimization minimizes the combined objective function  $\mathcal{L}$ , defined as a weighted sum of consistency loss (Equation 3) and the diffusion loss (Equation 6):

$$\mathcal{L} = \mathcal{L}_{\text{diffusion}} + \alpha \mathcal{L}_{\text{consistency}},\tag{11}$$

where  $\alpha$  is a hyperparameter balancing the two loss terms.

# C. Expert Demonstrations

Regarding the MetaWorld [59] and the RoboTwin [31] benchmarks, we utilize scripted policies to generate expert demonstrations. In the case of ManiSkill [14] tasks, we employ the officially provided demonstrations. Trajectories for other simulation benchmarks are collected with agents trained by RL algorithms [62, 43, 54]. The expert policies are evaluated over 200 episodes, and their success rates are detailed in Table XX.

Given the varying difficulty levels across benchmarks, we provide a different number of demonstrations for each. Specifically, we provide 50 trajectories per task for MetaWorld, Adroit, and RoboTwin. For DexArt, we follow the setup in [62] and provide 100 trajectories per task. For ManiSkill, we use all official demonstrations: 1000 for rigid tasks and 200 for deformable tasks.

In real-world experiments, we collect demonstrations of varying quantity, depending on the complexity and horizon length of the tasks. For short-horizon tasks, the number of collected trajectories is relatively limited — 100 for Clean Fridge and 200 for Place Bottle. In contrast, long-horizon tasks demand more comprehensive data coverage. We collect more demonstrations: 270 for Pour Juice and 500 for Sweep Trash. These demonstrations play a crucial role in guiding the training process, especially in scenarios where exploration is challenging or unsafe.

# D. Real-world Training Details

As mentioned in [13], DP-based methods often suffer from low inference speed, which can cause the inference process to stall. Prior approaches, including DP3 [62], attempt to address this by increasing action horizon (e.g.  $T_a = 4$  or  $T_a = 8$ ) or reducing the number of model parameters (e.g. Simple DP3). However, these strategies often compromise manipulation accuracy and dexterity. A further complication is that increasing  $T_a$  widens the temporal gap between consecutive inference steps, leading to greater discrepancies in observed information, and consequently, divergence in predicted actions. This often results in noticeable jitter and discontinuities in manipulation.

In general, DP-based methods are hindered by low inference speed, temporal inconsistency and overfitting to proprioceptive information. To address these challenges and improve real-world performance, we employ several empirical techniques.

1) Higher Inference Speed: To mitigate slow inference rooted in DP, we adopt an asynchronous design, achieving a final inference frequency of 10-15 Hz. Instead of waiting for the execution of all predicted actions before initiating the next inference cycle, our method performs inference concurrently with action execution. The predicted action

TABLE IX: Comparison of real-world inference speeds for different methods. The asynchronous version of our method demonstrates a significant speed-up by decoupling inference from action execution.

Method	DP	DP3	$H^3DP$	H <sup>3</sup> DP (asynchronous)
Inference Speed (FPS)	12.4	12.7	12.1	24.2

is stored in a queue to be executed at a fixed inference speed (10-15 Hz in practice, 12 Hz as average).

The inference speeds achieved in real-world scenarios are presented in Table IX. H<sup>3</sup>DP (asynchronous) demonstrates a superior inference speed compared to standard DP [6] and DP3 [62], as well as our synchronous H<sup>3</sup>DP implementation. In

addition to this speed advantage, H<sup>3</sup>DP features a shorter action sequence length  $(T_a = 2)$ , which contributes to more dexterous manipulation capabilities.

- 2) Temporal Consistency: Having adopted the asynchronous design, we have obtained action sequences with overlapping time intervals. To ensure temporal smoothness and reduce discontinuities, we incorporate temporal ensembling mechanism from ACT [65]. As in ACT, H<sup>3</sup>DP performs a weighted average of actions with the same timestep across multiple overlapping sequences. This ensembling mitigates the gap between actions inferred from slightly different observations and effectively reduces jitter.
- 3) Alleviate Overfitting: Similar to other real-world robotic systems, H<sup>3</sup>DP is susceptible to overfitting on proprioceptive inputs, often neglecting the RGB-D information. This is evidenced by that the model generates similar actions regardless of variations in object positions. We hypothesize that this occurs because the simple, low-parameter MLP used to encode proprioception is easier to optimize than the more complex CNN used for RGB-D input, leading to reliance on the former.

To mitigate this, we introduce a p-masking strategy during training. This mechanism stochastically masks all proprioceptive inputs with probability p, which decays linearly over the training process. Specifically, for training timestep t in a total horizon T, p(t) = 1 - t/T. This schedule encourages the model to rely more on RGB-D features early in training, helping it avoid early-stage overfitting and develop stronger visual grounding.

# E. Additional Experiment Results

1) Simulation Results for Each Task: We present the simulation results for each task in Table XIX, which serves as a supplement to Table I. For each experiment, we report the average success rate over three different random seeds. The final average result is obtained by averaging across all benchmarks.

We also provide the training progress of 4 algorithms on 12 various tasks across 3 different benchmarks in Figure 6. The selected tasks span a range of difficulties and are included without cherry picking to provide an unbiased view of each algorithm.

2) The Whole Results of Ablation Study: We present the entire results of our ablation study on each hierarchical design and number of layers N in Table X and Table XI, as a supplement to Table III and Table IV. For each experiment, the success rate is reported by averaging over 3 different random seeds. The final average result is obtained by averaging across benchmarks.

TABLE X: Whole results of ablation study on hierarchical features.

Method \ Tasks	Soccer	MetaW Stick Pull	aWorld     ManiSkill     RoboTwin       Il     Pick Out of Hole     Fill     Excavate     Tool Adjust		RoboTwin Tool Adjust	Average	
H <sup>3</sup> DP	85	<b>7</b> 5	37	98	38	45	59.6
w/o depth layering	59	72	34	78	27	32	46.5
w/o hierarchical action	64	67	40	82	18	40	49.0
w/o multi-scale representation	55	72	34	73	32	40	48.7
DP (w/ depth)	37	71	32	72	23	32	42.1

ManiSkill MetaWorld RoboTwin Method \ Tasks Average Stick Pull Pick Out of Hole Soccer Fill Excavate Tool Adjust  $H^{3}DP (N = 1)$ 59 72 34 27 32 46.5  $H^{3}DP (N = 2)$ 64 70 33 85 35 35 50.2  ${
m H^3DP}~(N=3)$ 75 37 45 **85** 98 38 **59.6**  $H^{3}DP (N = 4)$ 78 83 40 90 33 **50** 59.5  $H^{3}DP (N = 5)$ 75 39 87 23 **50** 62 54.6  $H^{3}DP (N = 6)$ 61 73 77 25 40 49.0

TABLE XI: Whole results of ablation study on number of layers N.

- 3) Comparison with a GMM-based Layering Variant: To highlight the advantages of depth-aware layering, we conduct a comparison against a variant where this module is substituted with a classical foreground-background segmentation method, Gaussian Mixture Models (GMM) [39], named H<sup>3</sup>DP-GMM. As shown in Table XII, H<sup>3</sup>DP outperforms H<sup>3</sup>DP-GMM in all benchmarks. Notably,  $H^3DP$ -GMM yields results comparable to a simple single-layer (N=1) approach, further emphasizing the rationality and effectiveness of our proposed depth-aware layering strategy.
- 4) Comparison with More Baselines: Except diffusion-based algorithms, we also compare H<sup>3</sup>DP with the recent state-of-theart method CARP [13], which uses multi-scale action VQ-VAE to build hierarchical action structures. Table XIII shows that H<sup>3</sup>DP outperforms CARP with an average improvement of 18.9%, indicating the importance of adopting hierarchical designs throughout visual features and action generation.

TABLE XII: Comparison with GMM-based layering variant. H<sup>3</sup>DP with depth-aware layering achieves superior performance compared to using GMM for layering.

Method \ Tasks	Soccer	MetaW Stick Pull	Vorld Pick Out of Hole	M   Fill	aniSkill Excavate	RoboTwin Tool Adjust	Average
$H^3DP$	85	83	40	98	38	45	64.8
H <sup>3</sup> DP-GMM	45	67	32	75	27	37	47.2
$\mathrm{H}^3\mathrm{DP}\ (N=1)$	59	72	34	78	27	32	50.3

TABLE XIII: Comparison with CARP. H<sup>3</sup>DP outperforms CARP with an average improvement of 18.9%.

Method \ Tasks	Box Close	Soccer	Stick Pull	MetaWorld Pick Out of Hole	Peg Insert Side	Hammer	Sweep	Average
$\mathrm{H}^3\mathrm{DP}$	98	85	83	40	98	100	100	86.3
CARP	82	53	71	15	69	82	100	67.4
DP	83	43	64	13	62	64	96	60.7

5) Comparison with DP with Pre-trained Visual Encoder: Prior work suggests that pre-trained visual representation may enhance spatial generalization of policy [58]. Hence, we investigate the impact of integrating a pre-trained visual encoder with the original DP. We specifically replace the standard ResNet encoder in DP with DINOv2 [32] model.

This variant, named DP-DINOv2, is evaluated on randomly selected tasks from the MetaWorld benchmark. The comparative results are presented in Table XIV. Although DP-DINOv2 shows a marginal improvement on some tasks compared to the original DP baseline, this comes with drawbacks, including a longer training time, inference latency and larger number of parameters(~21M for DINOv2 with ViT-S) due to the DINOv2 architecture.

In contrast, H<sup>3</sup>DP utilizes an efficient visual encoder with less than 0.7M parameters, which achieves strong performance improvements over the original DP without incurring the aforementioned overheads.

TABLE XIV: Comparison with DP with pre-trained visual encoder. While DP-DINOv2 yields small improvement after paying additional cost, H<sup>3</sup>DP demonstrates superior performance.

Method \ Tasks	Hand Insert	Pick Out of Hole	<b>MetaWorld</b> Disassemble	Stick Pull	Soccer	Sweep Into	Average
H <sup>3</sup> DP	100	40	96	83	85	100	84.0
DP	73	13	81	64	43	74	58.0
DP-DINOv2	91	24	77	72	41	78	63.8

6) Importance of Segmentation in DP3: As highlighted in Section IV-A2, DP3 relies on manual segmentation of point cloud for optimal performance. To demonstrate this dependency, we evaluate DP3's performance under two distinct segmentation conditions using randomly selected tasks from the MetaWorld benchmark.

We compare the following two scenarios: *DP3 with ideal segmentation*, which utilizes clean segmented point clouds containing only the robot and task-relevant objects, as implemented in the original DP3 algorithm; *DP3 without ideal segmentation*, which utilizes point clouds that are intentionally processed to include desk surface upon which objects rest, while other background elements are still removed. This configuration simulates common real-world scenarios where simple or automated segmentation rules might fail to perfectly isolate the task-relevant objects.

As shown in Table XV, DP3's performance degrades substantially when operating on point clouds without ideal segmentation. This result confirms that DP3 is highly sensitive to the quality of the input point cloud segmentation.

TABLE XV: Comparision of DP3 under different segmentation qualities. We compare DP3 success rates on selected tasks when provided with different segmentation qualities, highlighting significant performance degradation.

Method \ Tasks	MetaWorld							
Method \ Tasks	Push	Shelf Place	Stick Pull	Soccer	Bin Picking	Pick Place Wall	Average	
DP3	96	86	61	57	100	97	82.8	
DP3 (w/o ideal segmentation)	89	26	48	29	50	84	54.3	

In contrast, H<sup>3</sup>DP operates directly on raw image without requiring such pre-processing, thereby avoiding such failure mode and the associated need for careful, potentially manual, segmentation tuning, especially common in real-world scenarios.

7) H<sup>3</sup>DP in Tasks with Significant Depth Variations: As introduced in Section III-A, our depth-aware layering mechanism discretizes the depth map into distinct layers. This layering offers a crucial advantage in scenarios with significant depth

variations by providing a structured representation that preserves visual detail while emphasizing foreground-background separation. We will elaborate on this benefit and provide supporting comparative analysis here.

We conduct further experiments on tasks involving complex spatial arrangements, such as reaching for an object from closer to further or manipulating items in a cluttered scene, demanding a fine-grained understanding of relative object depth. Although raw RGB-D data contains this information implicitly, models may struggle to effectively utilize it, potentially treating the depth channel similarly to color channels or failing to prioritize significant depth discontinuities. Point cloud representations, inherently capturing 3D structures, often perform well in such scenarios as they directly encode geometric relationships.

Our depth-aware layering mechanism explicitly addresses this challenge for RGB-D inputs. By assigning pixels to discrete layers based on their depth values, we impose a structure that forces the model to differentiate between elements located at varying distances to camera. This discretization acts as an inductive bias, guiding the model to attend more strongly to the geometric layout and relative positioning of objects along the depth axis.

To empirically support our hypothesis, we conduct an ablation study focusing on tasks exhibiting significant depth variations. We compare the performance of three distinct approaches: DP3, DP (w/ depth) and H<sup>3</sup>DP (only with depth-aware layering, i.e., without hierarchical action and multi-scale representation).

As seen in Table XVI, our observations reveal a consistent pattern: in tasks involving significant depth variations, point cloud-based policy initially demonstrated superior performance compared to standard RGB-D processing, represented by DP (w/depth). However, upon integrating the depth-aware layering mechanism, H<sup>3</sup>DP consistently outperforms the baseline on these tasks, which strongly supports our claim.

TABLE XVI: **Performance comparison demonstrating the effectiveness of depth-aware layering.** Tasks with significant depth variations show great improvement only with depth layering compared to DP (w/ depth), surpassing the point cloud baseline (DP3).

Method \ Tasks	Push	Push Shelf Place Disassemble Soccer Pick Place Wall Peg Insert Side					
H <sup>3</sup> DP (only w/ depth layering)	100	95	98	55	100	86	89.0
DP (w/ depth)	79	29	76	37	80	53	59.0
DP3	96	86	98	<b>57</b>	97	92	87.7

8) Comparison with DP3 in Real-world Experiments: DP3 [62] is a renowned baseline succeeding DP [6] in imitation learning and robotic manipulation, achieving state-of-the-art results in multiple simulation environments. However, DP3 has notable limitations. In particular, it relies heavily on high-quality point clouds, typically requiring precision sensors such as the RealSense L515 to function effectively.

In our setup, the head-mounted camera is a ZED, which produces relatively low-quality visual inputs. This hinders the direct application of DP3 in our experimental setting. To ensure a fair comparison, we evaluate both H<sup>3</sup>DP and DP3 on two short-horizon real-world tasks both using the learning-from-scratch (LFS) encoder. The results are summarized in Table XVII.

It is evident that DP3 underperforms compared to H<sup>3</sup>DP in both tasks, highlighting H<sup>3</sup>DP's ability to robustly extract meaningful features from RGB-D inputs, even when the

TABLE XVII: Comparison of  $H^3DP$  and DP3 in real-world experiments. We make comparison in 2 short-horizon real-world tasks and both use LFS encoders.  $H^3DP$  achieves +29.0% performance gain.

Method \ Tasks	CF	PB	Average
H <sup>3</sup> DP	<b>51</b>	<b>52</b>	51.5
DP3	12	33	22.5

quality of visual input is suboptimal. Furthermore, we empirically find that employing spatially sparse convolution provides better performance than the DP3-style encoder, suggesting a promising direction for improving point cloud encoding in low-fidelity settings.

9) Inference Speed: As shown in Table XVIII, we evaluate the inference speed of different methods within simulated environments. The results indicate that the primary bottleneck of the inference speed of H<sup>3</sup>DP lies in the diffusion process itself, whereas the additional operations introduced for processing visual inputs and managing multi-scale representations incur only minimal computational overhead. A corresponding analysis of inference speed in real-world scenarios is available in Appendix D1.

TABLE XVIII: Comparison of inference speeds for DP, DP3 and H<sup>3</sup>DP in simulation tasks. The result indicates that additional operations introduced in H<sup>3</sup>DP are lightweight compared to the diffusion process.

Method	DP	DP3	H <sup>3</sup> DP
Inference Speed (FPS)	11.1	12.2	12.0

TABLE XIX: Success rates on 44 simulation tasks. Results of four different methods for each task are provided in this table. The summary across domains is shown in Table I.

	MetaWorld [59] (Medium)										
Method \ Tasks	Basketball	Bin Pic	king	Box Clos			offee Pusl	n Hamm	er So	ccer	Push Wall
$\mathrm{H}^{3}\mathrm{DP}$	100	100	100 98		100	100		100	8	85	100
DP	100	96		83	82		84	64		43	76
DP (w/ depth)	100	98		77	79		79	64	:	37	70
DP3	100	100		78	100		100	97	;	57	95
	Me	MetaWorld (Medium)					MetaV	World (Har	rd)		
Method \ Tasks	Peg Insert S	Side Swee	ep Sv	weep Into	Assembly	Hand I	nsert Pi	ck Out of	Hole	Pick Pl	ace Push
H <sup>3</sup> DP	98	100	)	100	100	100	0	40		99	100
DP	62	96		74	100	73		13		0	77
DP (w/ depth)	53	98		100	100	75		32		0	79
DP3	92	100	)	61	100	37		30		0	96
Mathed \ Teelre			Meta	World (Ha	rd++)			DexArt [2]			
Method \ Tasks	Shelf Place	Diassem	ole S	tick Pull	Stick Push	Pick Pl	ace Wall	Laptop	Faucet	Toile	et Bucket
$H^3DP$	100	96		83	100	1	.00	81	34	70	28
DP	20	81		64	70	:	55	69	23	58	27
DP (w/ depth)	29	76		71	100		80	63	20	62	23
DP3	86	98		61	100		97	80	33	<b>79</b>	27
Method \ Tasks	Adroit [36]				ManiSkill [14] (Rigid)						
,	Hammer I	Door Pen	Peg	Insertion S	side (Grasp)	Peg Insertion Side		e (Align)	Pick C	lube 7	Turn Faucet
H <sup>3</sup> DP	100	79 83		88			15		85		<b>73</b>
DP	95	69 73		78			7		17		8
DP (w/ depth)	100	66 62		93		12			33		23
DP3	100	71 81		63			12		10		48
Method \ Tasks	ManiSkil	(Deformab					RoboTwi				
Wiction \ Tasks	Excavate F	lang Pour	Fill	Apple C	abinet Storage	Dual	Bottles Pi	ck (Easy)	Dual I	Bottles 1	Pick (Hard)
H <sup>3</sup> DP	38	93 8	98		98		48			53	
DP	2	52 0	36		73		53			28	
DP (w/ depth)	23	78 7	72		2	33			25	25	
DP3	15	80 0	12		55		55			42	
Method \ Tasks	Block Hando	ver Block	: Hamn	ner Beat	<b>RoboTwin</b> Diverse Bottle	es Pick	Pick App	ole Messy	Tool A	Adjust	Average
H <sup>3</sup> DP	70		85		25			35	4	5	$75.6{\pm}18.6$
DP	28		0		0		0		-		48.1±23.1
DP (w/ depth)	0		0		2			7	3:	2	$52.8 \pm 22.2$
DP3	85		47		30			8	4		$59.3{\pm}24.9$

TABLE XX: Success rates of experts on 44 simulation tasks. We evaluate 200 episodes for each task. For ManiSkill tasks, the demonstrations are provided officially, and we record the success rates as 100%. The final average result is obtained by averaging across all benchmarks.

Method \ Tasks				MetaWorld [5	59] (Medium)				
Wiethod \ Tasks	Basketball	Bin Picl	king Box Clo	se Coffee Pu	ıll Coffee Pus	h Hamm	er Soccer	Push Wall	
Expert	100.0	97.0	90.0	100.0	100.0	100.0	90.5	100.0	
Made d \ Tesler	MetaWorld (Medium)				Meta	World (Hare	<b>d</b> )		
Method \ Tasks	Peg Insert Si	de Swee	p Sweep Into	Assembly	Hand Insert P	ick Out of I	Hole Pick	Place Push	
Expert	92.0	100.0	90.0	100.0	100.0	100.0	10	0.0 100.0	
	1		MetaWorld (Ha	ard++)			DexArt [2	 21	
Method \ Tasks	Shelf Place	Diassemb	`	,	Pick Place Wall	Laptop		oilet Bucket	
Expert	99.5	92.5	95.0	100.0	99.5	86.5	58.0 6	6.5 80.0	
	Adroit [	36]		ManiSkill [14] (Rigid)					
Method \ Tasks	Hammer Do	oor Pen	Peg Insertion	Side (Grasp)	Peg Insertion Sic	de (Align)	Pick Cube	Turn Faucet	
Expert	99.0 10	0.0 97.0	100	.0	100.0		100.0	100.0	
Made at \ Table	ManiSkill	(Deformabl	e)		RoboTw	rin [31]			
Method \ Tasks	Excavate Ha	ng Pour	Fill Apple	Cabinet Storage	Dual Bottles I	Pick (Easy)	Dual Bottle	es Pick (Hard)	
Expert	100.0 100	0.0 100.0	100.0	96.0	97.0	1	:	55.5	
Mathad \ Tasks				RoboTwin		•		Avorege	
Method \ Tasks	Block Hando	ver Bloc	k Hammer Beat	Diverse Bott	les Pick Pick A	Apple Mess	y Tool Ad	just   Average	
Expert	98.0		97.0	72.0		88.5	86.5	93.9	

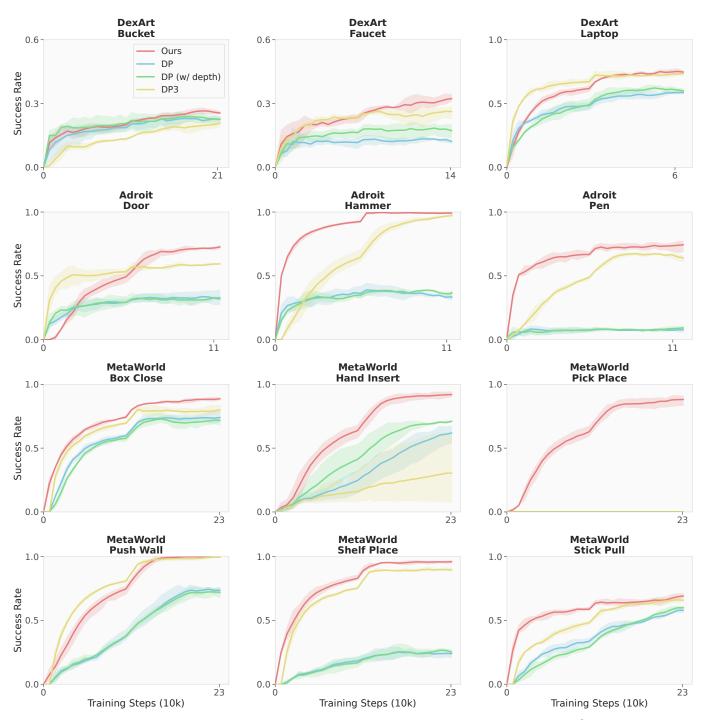


Fig. 6: Learning curves of the four methods on 12 randomly sampled diverse simulation tasks. In most tasks, H<sup>3</sup>DP demonstrates faster convergence, higher final success rates, and lower variance compared to other three methods.